Solving a, b, c from equations (14) and (20), we obtain the following calculated lattice parameters of the orthorhombic cell:

a=3.1460, b=4.7704, c=4.8510 kX.

The correspondence between the calculated and measured (X-ray) lattice parameters of the orthorhombic cell is very good for the a and c axes and fair for the b axis. The comparison does not take into consideration any lattice readjustment, such as homogeneous contraction (or expansion) parallel to certain crystallographic directions, which might take place during transformation. Thus, a homogeneous contraction by 0.015 kX. along the b axis of the orthorhombic cell will bring almost exact agreement between the calculated and measured lattice parameters of the orthorhombic phase.

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References

BARRETT, C. S. & TRAUTZ, O. R. (1948). Amer. Inst. Min. (Metall.) Engrs, Tech. Paper No. 2346. BURGERS, W. G. (1934). Physica, 's Grav., 1, 561.

- BYSTROM, A. & ALMIN, K. E. (1947). Acta Chem. Scand. 1, 76.
- CHANG, L. C. & READ, T. A. (1950). Amer. Inst. Min. (Metall.) Engrs, Tech. Paper No. 2941–E.
- COHEN, M. (1949). Trans. Amer. Soc. Met. 41, 35.
- GRENINGER, A. B. & TROIANO, A. R. (1949). J. Metals, 1, 590.
- GRENINGER, A. B. (1939). Trans. Amer. Inst. Min. (Metall.) Engrs, 133, 204.
- GRENINGER, A. B. & MOORADIAN, V. G. (1938). Trans. Amer. Inst. Min. (Metall.) Engrs, 128, 337.
- GRIDNEV, V. (1938). J. Tech. Phys. (U.S.S.R.), 5, 761.
- JASWON, M. A. & WHEELER, J. A. (1948). Acta Cryst. 1, 216.
- KURDJUMOW, G. & SACHS, G. (1930). Z. Phys. 64, 325.
- MEHL, R. F. & DERGE, G. (1937). Trans. Amer. Inst. Min. (Metall.) Engrs, 125, 482.
- NISHIYAMA, Z. (1934). Sci. Rep. Tôhoku Univ. 23, 637.
- ÖLANDER, A. (1932). Z. Krystallogr. 83, 145.
- SMITH, G. V. & MEHL, R. F. (1942). Trans. Amer. Inst. Min. (Metall.) Engrs, 150, 211.
- SMITH, C. S. (1950). Metal Progr. 58, 478.
- TROIANO, A. R. & MCGUIRE, F. T. (1943). Trans. Amer. Soc. Met. 31, 340.
- TROIANO, A. R. & TOKICH, J. L. (1948). Amer. Inst. Min. (Metall.) Engrs, Tech. Paper No. 2348.
- WASSERMANN, G. (1935). Mitt. K.-Wilh.-Inst. Eisenforsch. 17, 149.

Acta Cryst. (1951). 4, 324

The Crystal Structure of Lauric Acid

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Lauric acid (form C or α), $C_{12}H_{24}O_2$, is monoclinic with $\alpha = 9.524$, b = 4.965, c = 35.39 A., $\beta = 129^{\circ}$ 13'. The cell contains four molecules; density observed 1.032, calculated 1.034 g.cm.⁻³. The space group is $C_{2h}^5 - P2_1/a$. Fourier projections were prepared and atomic co-ordinates determined. The angle of tilt $\tau = 54^{\circ} 52'$.

Introduction

Lauric acid is known to exhibit polymorphism. Crystals of very pure lauric acid, prepared in these laboratories, were grown from ethanol solution. They proved to be in the form C of Francis & Piper (1939) or form α of Thibaud & Duprè de la Tour (1930*a*, *b*, 1932) with melting-point of 44.8°C. and setting-point 43.9°C.

Determination of X-ray data

The following data were determined from moving-film zero- and n-layer Weissenberg photographs about the

a and b axes and powder photographs using Ni-filtered Cu $K\alpha$ radiation:

Molecular formula $C_{12}H_{24}O_2$. Molecular weight = 200.31. The crystal is monoclinic with

$$a = 9 \cdot 524 \pm 0 \cdot 02,$$

$$b = 4 \cdot 965 \pm 0 \cdot 01,$$

$$c = 35 \cdot 39 \pm 0 \cdot 07 \text{ A.},$$

$$\beta = 129^{\circ} 13' \pm 1',$$

$$c \sin \beta = 27 \cdot 42 \pm 0 \cdot 06 \text{ A.}.$$

Four molecules per unit cell.

Density calc. = 1.034, density meas. = 1.032 g.cm.⁻³. Absent reflexions: (h0l) when h odd, (0k0) when k odd. Space group: $C_{2h}^5 - P_{2_1}/a$.

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Determination of the structure

The intensities of the reflexions were estimated by eye, using the multiple-film technique. During calculation of the observed structure factors, $|F_o|$, the normal

These projections revealed that the main cause of discrepancies between F_o 's and F_c 's had been the hydrogen atoms, which had not been included separately in the calculation of F_c 's.

| Table 1. Scattering curve for carbon and oxygen | | | | | | | | | |
|---|-----------------|-----------------|-----------------|-----------------|---------------|-----------------|-----------------|---------------|---------------|
| $\sin 	heta \ f$ | 0 1·000 | 0·05 0·957 | $0.10 \\ 0.850$ | $0.15 \\ 0.753$ | 0·20 0·656 | $0.25 \\ 0.553$ | $0.30 \\ 0.452$ | 0·35 0·350 | |
| $\sin_f \theta$ | $0.40 \\ 0.266$ | $0.45 \\ 0.203$ | $0.50 \\ 0.160$ | $0.55 \\ 0.128$ | 0·60 0·110 | $0.65 \\ 0.094$ | 0·70 0·080 | 0·75 0·063 | 0·77 0·055 |



Fig. 1. Lauric acid. Fourier projection along the b axis.

Lorentz and polarization correction factors were applied, together with Tunell (1939) geometrical correction factors for non-equatorial reflexions. Absolute values were obtained at a later stage by comparison with the calculated structure factors, F_c .

In the refinement of the structure a scattering curve for carbon and oxygen (Table 1) was constructed from comparisons of $|F_o|$ and $|F_c|$ values, and used in the calculation of F_c 's.

When calculating F_c values for zero-layer reflexions, with separate treatment of hydrogen atoms, the scattering curve of Morrison & Robertson (1949) was used.

Electron-density projections

A Fourier projection was made along the b axis, by addition of successive ripples starting with the strongest. Good resolution of the atoms was obtained and the z co-ordinates from this projection were used in the production of a projection along the a axis. Both were refined by the usual method of successive approximations. Line sections through some of the atoms, and a bounded projection along the a axis, were made, but the progress of refinement was slow.

Finally, difference maps, using $(F_o - F_c)$ as Fourier coefficients, were tried and proved very informative.



Fig. 2. Fourier projection along the a axis.

Fig. 3. A bounded section from $x = \frac{1}{4}$ to $x = \frac{3}{4}$ projected along the *a* axis.

Those hydrogen atoms not masked by carbon atoms in the projections appeared as positive peaks on the difference maps, and were then included in the structurefactor calculations, the remaining CH groups being assigned an effective atomic number of 7.

In the *a*-axis projection the carbon atoms were also moved in the directions of steepest ascent on a second difference map obtained with the new F_c values. The magnitude of the shifts was found by trial and error.

This treatment substantially reduced the figure of merit $\Sigma |F_o - F_c| \div \Sigma |F_o|$, from 26 to 21% for the *b*-axis projection and from 49 to 29% for the *a*-axis projection.

The final co-ordinates of the atoms are given in Table 2.

The hydrogen co-ordinates are those measured

directly on the difference maps, and are much less accurate than the co-ordinates of the carbon atoms. No attempt was made to adjust the carbon-hydrogen distances to fit the accepted bond length, or to refine the hydrogen co-ordinates.

As each hydrogen atom was resolved in only one projection, either the x or the y co-ordinate remains undetermined, and, in the calculation of the general structure factors, hydrogen atoms could not be included.

In Tables 3 and 4, the observed and calculated structure factors are given for the zero-layer and *n*-layer reflexions respectively. The F_c values were calculated by treating each CH₂ group as a single scattering unit, whereas $F_c(H)$ are structure factors calculated treating carbon and hydrogen atoms as separate.

Table 2. Co-ordinates of the atoms

| \mathbf{Atom} | x/a | y/b | z/c | Atom | x/a | z/c | Atom | y/b | z/c |
|-----------------|----------|--------|--------|-----------------|-------|-------|-------------------|-------|-------|
| OH | 0.3933 | 0.3000 | 0.0067 | H, | 0.300 | 0.059 | н. | 0.250 | 0.078 |
| C ₁ | 0.4513 | 0.4667 | 0.0429 | H, | 0.604 | 0.139 | H, | 0.747 | 0.128 |
| 0 | 0.5457 | 0.6533 | 0.0538 | H | 0.313 | 0.134 | H. | 0.247 | 0.155 |
| C_2 | 0.4000 | 0.3300 | 0.0750 | Н, | 0.604 | 0.208 | H | 0.753 | 0.203 |
| C_{s} | 0.4900 | 0.5267 | 0.1208 | H, | 0.333 | 0.208 | H_{10} | 0.253 | 0.236 |
| C_4 | 0.4217 | 0.3917 | 0.1483 | H_{11} | 0.650 | 0.288 | H_{12} | 0.753 | 0.280 |
| C ₅ | 0.5167 | 0.5600 | 0.1958 | H_{13} | 0.377 | 0.283 | H_{14} | 0.250 | 0.307 |
| C ₆ | 0.4467 | 0.4100 | 0.2242 | H ₁₅ | 0.704 | 0.367 | H_{16} | 0.747 | 0.340 |
| C, | 0.5433 | 0.5667 | 0.2739 | H ₁₇ | 0.380 | 0.353 | H_{18} | 0.247 | 0.372 |
| C ₈ | 0·4767 • | 0.4333 | 0.2992 | H ₁₉ | 0.714 | 0.437 | \mathbf{H}_{20} | 0.747 | 0.416 |
| C_9 | 0.5690 | 0.5733 | 0.3483 | H ₂₁ | 0.374 | 0.426 | H_{22} | 0.257 | 0.453 |
| C10 | 0.4983 | 0.4567 | 0.3742 | H_{23} | 0.560 | 0.479 | H_{23} | 0.753 | 0.479 |
| C_{11} | 0.5867 | 0.5633 | 0.4237 | | | | 20 | | |
| C_{12} | 0.5167 | 0.4533 | 0.4492 | | | | | | |

Table 3. (h0l) and (0kl) reflexions

| hkl | $ F_o $ | $F_{c}(\mathbf{H})$ | F_{c} |) hkl | Fo | $F_c(H)$ | F_{c} | hkl | $ F_{o} $ | $F_{c}(H)$ | F_{c} |
|------------|--------------|---------------------|--------------|--------|--------------|-------------------------|--------------|---------------------|--------------|------------|------------|
| 001 | 56.3 | 55.9 | 53.9 | 206 | < 2.8 | 1.5 | -1.8 | 2.0.20 | 7.1 | 4.3 | 8.0 |
| 002 | 13.1 | 18.1 | 19.9 | 207 | 4.3 | $\hat{0}\cdot\tilde{7}$ | 5.1 | 2.0.21 | ~ 3.8 | 2.2 | 2.0 |
| 003 | 41.6 | 42.2 | 40.5 | 208 | 4.4 | - 5.7 | 6.7 | 2.0.22 | 7.6 | 7.3 | 9.3 |
| 004 | <1.4 | 0.1 | - 5.7 | 209 | < 3.3 | 3.6 | 2.9 | 2.0.23 | ~ 3.9 | -1.2 | |
| 005 | $24 \cdot 4$ | 24.7 | 27.0 | | | | | 2.0.24 | 5.8 | 5.3 | 1.9 |
| 006 | 11.9 | -8.9 | -17.8 | 2.0.10 | 3.5 | -4.8 | - 7.6 | 2.0.25 | < 4.2 | - 1·9 | -0.9 |
| 007 | 11.0 | 15.3 | 17.8 | 2.0.11 | < 3.6 | 6.2 | 10.6 | $2.0.\overline{26}$ | 15.1 | 13.5 | 15.7 |
| 008 | $22 \cdot 2$ | $-22 \cdot 1$ | -20.1 | 2.0.12 | 31.6 | 31.0 | -40.8 | 2.0.27 | < 4.4 | 2.2 | 1.4 |
| 009 | 3∙4 | 6.1 | 8.8 | 2.0.13 | <3.9 | -6.5 | 0.0 | 2,0,28 | 25.5 | -24.1 | -24.7 |
| 0.0.10 | $27 \cdot 8$ | $-21 \cdot 2$ | -27.4 | 2.0.14 | 14.1 | 20.8 | 23.4 | $2.0.\overline{29}$ | 12.8 | -6.2 | -6.0 |
| 0.0.11 | 7.6 | 5.7 | $11 \cdot 2$ | 2.0.15 | 5.9 | 5.5 | 4 ·0 | 2.0.30 | 12.7 | - 8.9 | - 10.6 |
| 0.0.12 | 4 0·7 | -34.0 | -38.8 | 2.0.16 | 6.1 | 11.3 | 16.3 | 2.0.31 | 6.3 | -4.6 | - 3.9 |
| 0.0.13 | 4 ·3 | 2.8 | - 1.3 | 2.0.17 | <4.4 | 5.6 | -4.6 | $2.0.\overline{32}$ | < 4.4 | -3.2 | -4.2 |
| 0.0.14 | 51.1 | 42·8 | 44 ·0 | | | | | | | | |
| 0.0.15 | 9·4 | 8.5 | 4.6 | 201 | 11.6 | 9.4 | $2 \cdot 0$ | 400 | 14.8 | 16.4 | 22.8 |
| 0.0.16 | 14.0 | 10.8 | 16.0 | 202 | 68 .0 | 70.1 | -86.9 | 401 | <3.4 | -10.0 | -7.5 |
| 0.0.17 | 10.3 | 8.6 | 7.9 | 203 | 20.9 | 13.8 | 17.8 | 402 | < 3.5 | 3.7 | 4.2 |
| 0.0.18 | 7.6 | 6.4 | 3.5 | 204 | $23 \cdot 6$ | -20.6 | 30.0 | 403 | < 3.6 | -8.2 | -12.2 |
| 0.0.19 | $7 \cdot 9$ | 4.9 | $2 \cdot 2$ | 205 | 11.8 | 6.6 | 7.3 | 404 | 5.3 | - 1.6 | -0.8 |
| 0.0.20 | 8.2 | 4 ·2 | 3 ∙5 | 206 | 18.7 | -17.6 | $28 \cdot 8$ | 405 | <3.9 | -7.5 | -6.3 |
| 0.0.21 | 6.0 | 5.5 | 4.1 | 207 | <1.9 | 0.6 | 0.0 | 406 | <4 | -1.5 | 0.1 |
| 0.0.22 | <4.3 | 3.7 | 7.7 | 208 | 31.1 | $-24 \cdot 2$ | -25.8 | 407 | <4 | -4.6 | -2.4 |
| 0.0.23 | <4.3 | 1.4 | 1.7 | 209 | 16.2 | -15.2 | -11.0 | 408 | 6.0 | - 1.3 | -1.5 |
| 0.0.24 | <4.4 | 2.8 | 0.4 | 2.0.10 | 30.9 | -26.0 | -33.5 | 409 | <4 | 0 | -1.3 |
| 0.0.25 | < 4.5 | -0.1 | 1.4 | 2.0.11 | · 20·8 | -15.6 | -16.2 | 4.0.10 | <4.4 | 3.0 | 4.6 |
| 0.0.26 | 12.7 | 12.3 | 11.4 | 2.0.12 | 34.5 | -24.5 | -25.9 | 4.0.11 | < 4.5 | 5.4 | 6.5 |
| | | | | 2.0.13 | $22 \cdot 8$ | -18.7 | -24.0 | 4.0.12 | 15.6 | -25.7 | -29.6 |
| 200 | 190.5 | 184.9 | 212.5 | 2.0.14 | 20.6 | -24.2 | -15.4 | | | | |
| 201 | 37.5 | 19.7 | 19.2 | 2.0.15 | 19.6 | -12.5 | -17.5 | 401 | 9.1 | -11.2 | 14.8 |
| 202 | 47.3 | 41 ·2 | 47.6 | 2.0.16 | 8.4 | -7.2 | -4.2 | $40\overline{2}$ | 44 ·0 | -40.1 | -50.2 |
| 203 | 7.0 | 1 0·3 | 3.6 | 2.0.17 | < 3.1 | -2.2 | -4.0 | 403 | <3.1 | -3.8 | -3.4 |
| 204 | 7.4 | 12.8 | 11.3 | 2.0.18 | < 3.2 | $2 \cdot 2$ | -0.5 | $40\overline{4}$ | 3.0 | -10.3 | - 5.6 |
| 205 | < 2.8 | $2 \cdot 5$ | $4 \cdot 2$ | 2.0.19 | < 3.4 | -0.3 | - 2.2 | 405 | < 2.9 | - 5.7 | -4.0 |

Table 3 (cont.)

| hkl 406 | F _o 2.9 | $F_c(\mathrm{H})$ -9.2 | F_c -10.7 | hkl $6.0.\overline{21}$ | $ F_o $ < 3.9 | F _c (H) 2.7 | F_c -0.3 | hkl 021 | $\mid F_o \mid$ 17·2 | $F_c(\mathbf{H}) = -30.1$ | F_c - 35.9 |
|--|--|--|----------------------------|--|---|-----------------------------|---|---|---------------------------------|---------------------------|--|
| 407 408 | 2·8 17·8 | -7.9 -15.9 | -7.4 -13.2 | $\begin{array}{c} 6.0.\overline{22} \\ 6.0.\overline{23} \\ 6.0.\overline{23} \end{array}$ | < 4.0 < 4.0 | 7.6 4.2 | 3·5 2·5 | 022 023 024 | $27.4 \\ 12.5 \\ 17.0$ | -25.1 -9.2 | -29.4 -13.2 -22.0 |
| 409 4.0. <u>10</u> 4.0. <u>11</u> | 17.8 24.9 25.2 | -21.5 -22.6 -20.7 | -13.0 20.8 -20.0 | 6.0.24 6.0.25 6.0.26 | $5.8 \\ 5.9 \\ < 4.2$ | 4·1 4·9 1·3 | 4·7 6·8 1·0 | 024 025 026 | 5.8 8.3 | -18.3 -0.5 -8.3 | -22.0 0.9 -8.8 |
| 4.0.12 | 44·0 36·4 | -36.3 -24.4 | -31.6 -27.4 | 6.0.27 6.0.28 | 6.1 34.0 | 6.0 - 23.7 | 6.4 - 29.3 | 027 | 3·0 4·4 | 5.1 - 6.0 | 8.1 - 5.8 |
| 4.0.13 4.0.15 | 90.6 37.8 | -82.5 -22.2 | -76.3 -22.1 | $6.0.\overline{29}$ $6.0.\overline{30}$ | < 4.4 8.9 | 0·4 10·0 | 1.5 10.3 | 029 | $< \frac{3 \cdot 1}{4 \cdot 7}$ | 1.0 - 8.6 | 3·1 |
| 4.0.16 | 8.6 14.3 | 19·7 | 13.6 - 12.0 | 6.0.31 | < 4.5 | -1.3 | -1.7 | 0.2.11 | $3.4 \\ 29.7$ | -3.0 -25.8 | -0.7 -29.9 |
| 4.0.18 | 4·6 | 7.7 _ 3.4 | 8·1 4·3 | 8.0. <u>16</u> 8.0. <u>29</u> | $20.0 \\ 6.4$ | $27 \cdot 1 \\ 3 \cdot 2$ | $33 \cdot 4 \\ 4 \cdot 8$ | 0.2.13 | 19.4 < 3.8 | -17.0 -2.3 | -16.8 0.8 |
| 4.0.20 4.0.21 | 4.9 < 3.5 | 6·1 0·1 | -12.8 -1.7 | 010 | 0 | 0 | 0 | 0.2.15 | $5 \cdot 5$ | -8.3 | - 9·6 |
| $4.0.\overline{22}$ $4.0.\overline{23}$ | 5·1 < 3·8 | 9.2 - 2.8 | 7.8 - 2.1 | 011 012 | $10.3 \\ 20.5$ | -10.0 -18.9 | -8.1 -8.3 | 030 031 | 0 < 3.8 | 0.4 | 0 0 |
| $4.0.\overline{24} \\ 4.0.\overline{25}$ | 5.5 < 4.0 | 5.4 - 0.7 | $4 \cdot 2 \\ - 0 \cdot 3$ | 013 014 | $12 \cdot 2$ $2 \cdot 9$ | $-5.2 \\ 0.2$ | $-2.5 \\ 3.0$ | 032 033 | < 3·8 < 3·8 | $-1.0 \\ 1.5$ | $-\frac{1\cdot 2}{1\cdot 0}$ |
| 4,0, <u>26</u> 4,0, <u>27</u> | 5.8 < 4.3 | 4∙0 1∙1 | $8\cdot 3$ $1\cdot 1$ | 015 016 | < 1.9 < 2.2 | 0·4 4·8 | $\begin{array}{c} 0 \\ 8\cdot7 \end{array}$ | 034 035 | < 3.8 < 3.8 | 2.3 - 0.5 | 1·6 1·4 |
| 4 <i>.</i> 0 <i>.</i> 28 4 <i>.</i> 0 <i>.</i> 29 | $69.9 \\ 17.8$ | -37.3 -8.5 | $-40.8 \\ -6.2$ | 017 018 | $<\!$ | $2 \cdot 7$ $3 \cdot 5$ | 1∙0 3∙6 | 036 037 | $3 \cdot 7$ $3 \cdot 8$ | $2 \cdot 1 - 2 \cdot 1$ | $3 \cdot 4$ $2 \cdot 2$ |
| 4 <i>.</i> 0. <u>30</u> 4.0. <u>31</u> | $< 4.5 \\ 6.4$ | $-3 \cdot 2 \\ -5 \cdot 4$ | -5.8 -5.2 | 019 0.1.10 | 11.7 < 2.7 | $-rac{7\cdot 6}{0\cdot 3}$ | -7.8 -6.6 | 038 039 | < 3.8 < 3.8 | -0.3 - 5.4 | $1 \cdot 1 - 5 \cdot 6$ |
| 6.0.12 | < 3.7 | | -16.1 | 0.1.11 0.1.12 | $4 \cdot 1 \\ 13 \cdot 3$ | $-6.8 \\ 16.4$ | $-9.2 \\ 16.0$ | $0.3.10 \\ 0.3.11$ | $< 4 \cdot 1$ $< 4 \cdot 4$ | -0.3 - 3.4 | -1.4 - 3.6 |
| 6.0. <u>13</u> 6.0. <u>14</u> | $< 3.7 \\ 28.5$ | -4.5 -29.7 | -5.9 -35.7 | 0.1.13 0.1.14 | $< 3.2 \\ 42.3$ | $-4 \cdot 1 \\ -40 \cdot 2$ | -4.8 -35.9 | $\begin{array}{c}0.3.12\\0.3.13\end{array}$ | 5.9 < 4.2 | $16.7 \\ 5.6$ | $ \begin{array}{r} 19.6 \\ 6.2 \end{array} $ |
| 6.0. <u>15</u> 6.0. <u>16</u> | $< 3.8 \\ 31.3$ | $-0.7 \\ 24.6$ | $-2.4 \\ 40.3$ | 0.1.15 0.1.16 | $4 \cdot 9 \\ 5 \cdot 1$ | -9.0 -11.1 | $-12 \cdot 2$ $-13 \cdot 0$ | 0,3,14 | 6.1 | - 19.3 | - 21.9 |
| 6.0.17 6.0. <u>18</u> | <3.8 <3.8 | -0.1 8.3 | -5.6 10.2 | 0,1,17 0,1,18 | $3 \cdot 7$ $< 3 \cdot 9$ | -6.4 - 3.7 | -6.3 - 4.3 | 048 049 | $4 \cdot 4$ $6 \cdot 3$ | 4·4 3·7 | 2·8 2·7 |
| 6.0.19 6.0.20 | < 3.8 < 3.9 | $\begin{array}{c} 0.8\\ 6.1 \end{array}$ | 0·2 8·1 | 020 | 48 ·6 | 51 ·3 | 79·3 | 0,4,10 | $6.3 \\ 4.5$ | 3.9 4.1 | $\frac{2\cdot 5}{3\cdot 2}$ |
| | | | | Table | e 4. Gen | eral refle: | xions | | | | |
| hkl | $ F_{o} $ | 1 | F_{c} | hkl | F | 0 | F _c | hkl | F | 0 | F _c |
| $\begin{array}{c}110\\111\end{array}$ | 152 10 | ·3 ·1 | 233.5 1.7 | 210 | 64 33 | ₽•6 3•6 | 73.9 51.5 | 311 312 | 5 | ·1 ·4 | 1.9 15.9 |
| $\frac{112}{113}$ | <1 <1 | ·3 ·8 | 17·6 1·8 | 212 213 | 23 17 | 3.9 1.5 | 19·3 23·2 | 313 314 | < 2 < 3 | ·5 ·1 | $-\frac{8\cdot 2}{2\cdot 7}$ |
| 114 115 | 1 < 2 | .9 ·5 | -6.3 5.9 | 214 215 | 12 | 2·4 | 8.2 11.6 | 315 | 3 < 3 | •1 •1 | 2·8 1·9 |
| 116 117 | $10^{-10^{-10^{-10^{-10^{-10^{-10^{-10^{-$ | -7 | - 8·0 10·7 | 216 | 5 4 | 0.8 1.3 | 3.6 6.5 | 3,1,12 | 14 | | 30.9 |
| 118 | <3 | -1 | - 10.7 5.9 | 218 | < 3 | 3·1 3·3 | 0.8 | | < 2 28 | · 1 · 5 | -4.2 -54.5 |
| 1,1,10 | <3 | ·4 ·1 | - 14·8 8·5 | 2,1,10 | < 3 | 3·5 3·8 | -4.0 -0.9 | $313 \\ 314 \\ 31\overline{4}$ | < 2 | ·1 ·3 | -12.1 |
| 1,1,12 | 33 [.] 9. | ·1 ·7 | -38.8 -6.3 | 2,1,12 2,1,13 | 4 | 1.0 | 12·0 4·4 | | < 2 | -5 -5 | -12.4 |
| 1/1/14 | 10 | .0 | 21.1 | 211 | 47 | 7·0 | 41·4 | | 4 | -7 -8 | -11.5 -7.3 |
| 112 | 22 | ·5 | -46.5 | 212 213 213 | 30 |)•8 1.5 | 24.2 | 3,1,10 | 12 | -9 -2 | -14.2 |
| 113 | 9- 9- | ·1 | -24.8 | | 10 |)·6 | 6.9 - 8.7 | 3,1,12 | 16 16 7 | -2 -6 | -17.4 -13.9 |
| 115 | 10- | ·5 | - 19.5 | 217 | 5 | 5·5 2.0 | $1 \cdot 2$ - 5 \cdot 7 | 3,1,14 3,1,15 | 32 4 | ·5 ·0 | -34.5 -4.5 |
| 118 | 17- | .4 .2 | -19.7 -0.5 | | 9 < 2 |)·4 2·2 | 9·6 4·4 | $\begin{array}{c}3.1.\overline{16}\\3.1.\overline{17}\end{array}$ | 10 3 | ·2 ·1 | 11·8 0·4 |
| | $2\overline{5}$ | -0 -0 | -26.8 -5.2 | $\frac{2.1.\overline{11}}{2.1.\overline{12}}$ | 12 | 2.3 3.5 | $1\overline{1\cdot8}$ $2\cdot4$ | $3,1,\overline{18}$ $3,1,\overline{19}$ | 11 4 | ·1 ·7 | $8.5 \\ 0.1$ |
| $1,1,\overline{12}$ $1,1,\overline{13}$ | 37- 19- | ·2 ·8 | -32.8 -13.5 | $2.1.\overline{13}$ $2.1.\overline{14}$ | 7 91 | 1·4 1·6 | $19.4 \\ 73.3$ | $3.1.\overline{20}$ $3.1.\overline{21}$ | 6 5 | 9 1 | 8·3 0·9 |
| $1,1,\overline{14}$ $1,1,\overline{15}$ | 12 < 3 | -9 -0 | 16.4 - 2.8 | $2.1.\overline{15}$ $2.1.\overline{16}$ | 20 |)•6 3•0 | 20·0 9·1 | $\begin{array}{c} 3,1,\overline{22}\\ 3,1,\overline{23} \end{array}$ | 5 < 3 | ·3 ·8 | $7 \cdot 6 \\ -1 \cdot 2$ |
| $1.1.\overline{16}$ $1.1.\overline{17}$ | <3 4 | -1 -7 | $5.5 \\ 2.3$ | $2.1.\overline{17}$ $2.1.\overline{18}$ | 10 4 |)·8 •6 | 10·4 4·4 | $\begin{array}{c} 3.1.\overline{24} \\ 3.1.\overline{25} \end{array}$ | 5 < 4 | ·6 ·1 | $5 \cdot 0 - 0 \cdot 2$ |
| 1,1, <u>18</u> 1,1, <u>19</u> | 7-7-7- | ·0 ·3 | $-3.8 \\ 0.1$ | $\begin{array}{c} 2.1.\overline{19} \\ 2.1.\overline{20} \end{array}$ | 6 5 | 3·8 5·1 | 4·3 0·4 | $\begin{array}{c} 3.1.\overline{26} \\ 3.1.\overline{27} \end{array}$ | 11 6 | •8 •1 | $14.3 \\ 3.3$ |
| $1.1.\overline{20}$ $1.1.\overline{21}$ | 5.5 | •4 •7 | 3∙4 3∙3 | 310 | 49 |)•3 | 71.9 | $\begin{array}{c} 3.1.\overline{28} \\ 3.1.\overline{29} \end{array}$ | 27 6 | ·8 ·3 | -28.1 -1.4 |

| | | | г | able 4 (con | et.) | | | |
|--------------------------|--------------|--------------|------------------|-------------------------------------|---------------------------------|-------------------------------|------------------------|------------------------|
| hkl | $ F_{o} $ | F_{c} | hkl | $ F_{o} $ | F, | hkl | $ F_{a} $ | F. |
| 410 | 22.1 | 29.3 | 133 | < 3.8 | -2.1 | 327 | 5.5 | _ 1·1 |
| 411 | 11.9 | 12.8 | 1,3,11 | < 3.8 | $\overline{0}\cdot\overline{3}$ | 328 | 9.9 | $-\hat{6}\cdot\hat{8}$ |
| 412 | 12.2 | 14.3 | 1,3,12 | 8.0 | -15.7 | $32\overline{9}$ | 8.0 | 1.1 |
| 413 | 0.2 11.3 | 10.1 | 1,3,13 | 5.7 | - 10.3 | 3,2,10 | 8.0 | - 1.3 |
| 412 | < 3.2 | -17.0 | 220 | 29.2 | 54.5 | 3,2,11 | 0°8 5.9 | - 1.1 |
| 413 | 8.7 | 5.1 | 221 | 4.2 | -17.5 | 3.2.13 | 4.3 | 3.9 |
| 414 | < 3.1 | -4.3 | 222 | 8.6 | 1.5 | 3.2.14 | 27.8 | 58.5 |
| 415 418 | < 3·1 5.9 | 2.9 | 223 | 14.0 | -11.8 | 3.2.15 | < 3.1 | 4.8 |
| 417 | 3·8 8·1 | -4.8 | 224 | 9·1 4·7 | 5.3 | 3,2,16 | 11.4 | 10.4 |
| 418 | 8.0 | -7.4 | 2,2,12 | 23.5 | -22.7 | 330 | 5.5 | 11.1 |
| 419 | 5.6 | -4.8 | 2.2.13 | 4 ·2 | -7.6 | 3,3,15 | 4.0 | 14.5 |
| 4,1,10 | 4.0 | 3.3 | 0.07 | . 0 1 | F 4 | 3,3,16 | 11.5 | 19.0 |
| $\frac{4}{1}$ | < 3.1 | - 5·0 4·2 | 221 | < 3·1 17·9 | - 7.4 | 3411 | - 1.1 | 4.4 |
| 4.1.13 | < 3.1 | 1.7 | 223 | 11.2 | 7.0 | 3.4.12 | 8.7 | - 7.3 |
| 4,1,14 | 25.0 | 34.6 | 224 | < 2.5 | -12.9 | 3,4,13 | 8.7 | 11.5 |
| 4,1,15 | < 3.1 | -2.4 | 225 | 7.8 | 4.9 | 3.4.14 | 8.8 | 17.2 |
| 4.1.17 | 20.4 | - 19.1 | 226 | < 2.5 | -7.3 | 3,4,15 | < 4.4 | -7.8 |
| 4,1,18 | < 3.1 | -3.3 | 228 | < 2.7 < 2.9 | - 3.8 | 3,4,16 | 8.8 | - 9.5 |
| 4,1,19 | <3.4 | -0.4 | 229 | $< \overline{3} \cdot \overline{1}$ | 0.6 | 420 | 15.5 | 20.8 |
| 4,1,20 | < 3.4 | -0.6 | 2.2.10 | 4 ·2 | -6.2 | 421 | 3.6 | 2.8 |
| 4.1.30 | 6.3 | -5.7 | 2,2,11 | 6.0 | -2.4 | | <u> </u> | |
| 5.1.14 | 27.9 | 37.8 | 2,2,12 | 19.2 | - 16.3 | 421 | 6.7 | 6.5 |
| 5,1,16 | 25.0 | 32.3 | 2.2.13 | - 3·1 | - 7.8 | 422 | < 3·1 9.1 | -7.0 |
| 5.1.28 | 34 ·0 | 30.6 | 2.2.15 | 6.7 | 7 .1 | 424 | 3.1 | -4·1 |
| 017 | • | | 2.2.16 | 15.6 | 14.5 | 425 | 4.3 | 0.3 |
| 619 61 TG | < 3·8 | - 6.9 | 2.2.17 | 12.5 | 6.7 | 426 | 4.3 | - 3.5 |
| 6.1.11 | < 3.8 | 10.1 | 2,2,18 | 10.5 | 6·1 9.0 | 427 | 4.3 | -3.2 |
| 6.1.12 | 7.4 | -5.5 | 2.2.20 | 5.6 | 2.0 | 428 | 4.3 | 3.1 |
| 6,1,13 | <3.8 | -8.5 | 2.2.21 | < 3.8 | 0.1 | 4,2,10 | $<\hat{3}\cdot\hat{1}$ | 2.8 |
| 6,1,14 | 7.3 | -3.3 | 2.2.22 | <4.0 | 4 ·0 | 4,2,11 | $< 3 \cdot 1$ | 5.4 |
| 0,1,15 6 1 <u>9 9</u> | 10.4 | - 10.5 | 2,2,23 | <4.2 | -0.9 | 4.2.12 | < 3.1 | -1.8 |
| $6,1,\overline{29}$ | 6.2 | | 2,2,24 | < 4·4 ~ 4·5 | 3.8 | 4,2,13 | 8.7 | 10.1 |
| | • - | 01 | 2.2.26 | 8.9 | 8.5 | 4,2,14 4,2,15 | 14.1 | 16.8 |
| $7,1,\overline{16}*$ | 18.6 | 32.9 | 2.2.27 | < 4.5 | 4.3 | 4.2 16 | 24.9 | 25.3 |
| 7.1.28 | 12.5 | -17.9 | 2.2.28 | 8.9 | -8.9 | 4.2.17 | 11.4 | 4.9 |
| 120 | 94.7 | 40.4 | 990 | 10.5 | 16.7 | 4,2,18 | 9.6 | 8.6 |
| 120 | 4.0 | ±0°± 6·1 | 230 | 10.5 | 10·7 | 4,2,19 | < 3.8 | 0 |
| 122 | <3.1 | -2.7 | 239 | 5.2 | -4.8 | 4.2.21 | < 3.8 | 2.8 |
| 123 | < 3.1 | 5.2 | 2,3,10 | $6 \cdot 2$ | - 7.9 | 4.2.22 | < 3.8 | 3.2 |
| 124 | 3.0 | 2.4 | 2,3,11 | 4.4 | -6.2 | 4.2.23 | < 3.8 | -1.2 |
| 125 | 3·1 < 3·2 | 1·9 5·0 | 0.97 | × 9.0 | 4.9 | 4,2,24 | 5.6 | 4.3 |
| 127 | < 3.4 | 1.1 | 231 | < 3.8 7.3 | | 4,2,25 A 9 $\overline{96}$ | 4·1 11.7 | 2.9 |
| 128 | <3.6 | 1.4 | 233 | < 3.8 | 1.6 | 4.2.27 | 8.4 | 8.2 |
| 129 | < 3.8 | 5.2 | $23\overline{4}$ | 10.2 | -6.4 | 4,2,28 | 17.0 | -15.2 |
| 1,2,10 | 5·0 ~ 3.8 | - 6.1 | 235 | 10.1 | 2.7 | 100 | | |
| 1.2.12 | 5.4 | 19.9 | 230 | 10.1 | - 0.0 | 430 | 11.5 | 15.9 |
| 1.2.13 | 5.5 | 3.2 | 238 | 10.4 | -4.2 | 432 | 3.9 | -20.0 |
| 1,2,14 | < 3.8 | 16.3 | 239 | $5 \cdot 2$ | 1.9 | 433 | 3.9 | 9.1 |
| 1,2,15 | 5.8 | 1.8 | 2,3,10 | 10.6 | -5.9 | 434 | < 3.8 | 0.5 |
| 121 | 12.3 | 17.8 | 2,3,11 | 5.3 20.3 | - 5.7 | 435 | < 3.8 | 3.2 |
| $\overline{122}$ | 7.7 | 10.9 | 2.3.13 | 17.6 | -12.4 | 430 | < 3.8 | - 2.5 |
| 123 | 5.5 | 10.0 | 2,3,14 | 21.1 | 30.4 | 438 | < 3.8 | -1.1 |
| 124 195 | 3.8 | 4.4 | 2.3.15 | < 4.4 | -9.3 | 4 <u>3</u> <u>9</u> | < 3.8 | -1.4 |
| 125 | 3.9 8.0 | - 10.8 | 2,3,16 | 16.5 | - 10.4 | 4,3,10 | < 3.8 | -3.4 |
| 127 | 4 ·0 | $1\cdot 2$ | 2,4,19 | 4.4 | -1.7 | 4.3.11 | 3.8 | - 3.0 |
| $12\overline{8}$ | 5.9 | -6.6 | 2,4,20 | 4.4 | -2.9 | 4,3,13 | 3.8 | - 8.4 |
| 129 | <3.1 | 7.0 | 2,4,21 | 4.3 | -2.6 | 4,3,14 | 10.9 | 24.7 |
| 1,2,10 | < 3.1 | -1.0 | 200 | 04.1 | 41.0 | 4.3 15 | < 3.8 | -2.9 |
| 1.2.12 | 18.6 | - 19.8 | 320 | 34.1 | 41.0 | 4,3,16 | 13.6 | -14.2 |
| $1.2.\overline{13}$ | 6.8 | 1.3 | 322 | 6.6 | - 11·6 | 4.3.18 | < 3·8 4·0 | - 3.4 |
| 1,2,14 | 49·3 | 51.8 | 3,2,10 | 4.2 | -6.7 | 4.3.19 | 11.5 | 2.4 |
| 180 | 7.0 | 7.0 | 997 | 10.4 | 10.0 | 4.3.20 | 8.2 | 1.7 |
| 131 | 7-2 5-1 | - 19.2 | 321 | 13.4 | 10.0 | 4,3,21 | $4 \cdot 2$ | 5.0 |
| 132 | 7.3 | -8.7 | 323 | 8.2 | 6.9 | 4.4.18 | 8.5 | - 1.5 |
| 107 | . . | | $32\overline{4}$ | < 3.1 | -9.1 | 4.4.19 | 8.5 | -2.0 |
| 131 | 5·0 7.1 | - 13.7 | 325 | <3.1 | -0.3 | 4.4.20 | 8.5 | -2.9 |
| 104 | 1.1 | -0.0 | 1 320 | 9.9 | -11.3 | | | |

* May be 7.1.15

Discussion of the results

Closer examination of the projections revealed that in lauric acid the hydrocarbon chain is not quite straight. It is noticeably bent in the *a*-axis projection. The average vector between alternate carbon atoms has been calculated by the least-squares method; its components are given in Table 5, in which the linear term in the y component is due to the curvature of the chain. The co-ordinates of the atoms in the carboxyl group are not sufficiently accurate to warrant a detailed discussion of the bond lengths; however, it can be seen that, as in dicarboxylic acids recently studied by Robertson and co-workers, the two C—O and C=O bonds are of unequal length, being 1.38 and 1.17 A., respectively.

The molecules are joined in pairs by hydrogen bridges 2.56 A. in length between the double-bond oxygen of

Table 5. Components of average vector between alternate carbon atoms

| Co-ordinate | Fractional components | |
|------------------|--|--|
| x | 0.02473 ± 0.0005 | |
| \boldsymbol{y} | $(0.0644 \pm 0.005) - (0.0068 \pm 0.0006) N$ | |
| z | 0.0752 ± 0.0001 | |

The angles of constant direction, as defined by Vand, Aitken & Campbell (1949), are $\alpha_o = 92^{\circ}28'$, $\beta_o = 125^{\circ}1'$, and the angle of tilt $\tau = 54^{\circ}52'$.



Fig. 4. Perpendicular projection of the oxygen atoms on the ab plane. The oxygen atoms marked (+) or (-) are 1.48 A. above or below the ab plane, the unmarked atoms approximately in that plane.

The average distance between alternate carbon atoms is $s=2.521\pm0.007$ A. This is significantly shorter than the distance in soaps, namely, 2.610 A., found in strontium laurate by Morley & Vand (1949) and 2.598 ± 0.007 A. found in potassium caprate by Vand, Lomer & Lang (1949). One can thus conclude that this distance varies from compound to compound. It is probable that it depends on the compression forces within the crystal; a lateral compression would tend to elongate the zigzag hydrocarbon chains. Rectangular components (A.) -1.4470 ± 0.006 $(0.319 \pm 0.025) - (0.0338 \pm 0.003) N$ 2.0617 ± 0.005

the upper molecule and the single-bond oxygen of the lower molecule and vice versa. The packing of the carboxyl groups is shown in Fig. 4.

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References

- FRANCIS, F. & PIPER, S. H. (1939). J. Amer. Chem. Soc. 61, 577.
- MORLEY, W. M. & VAND, V. (1949). Nature, Lond., 163, 285.
- MORRISON, J. D. & ROBERTSON, J. M. (1949). J. Chem. Soc. p. 933.
- THIBAUD, J. & DUPRÈ DE LA TOUR, F. (1930a). C.R. Acad. Sci., Paris, 190, 945.
- THIBAUD, J. & DUPRÈ DE LA TOUR, F. (1930b). C.R. Acad. Sci., Paris, 191, 200.
- THIBAUD, J. & DUPRÈ DE LA TOUR, F. (1932). J. Chim. phys. 29, 153.
- TUNELL, G. (1939). Amer. Min. 24, 448.
- VAND, V., AITKEN, A. & CAMPBELL, R. K. (1949). Acta Cryst. 2, 398.
- VAND, V., LOMER, T. R. & LANG, A. (1949). Acta Cryst. 2, 214.